

CLASS TEST-2
CHAPTER-SEQUENCE AND SERIES (CLASS XI)

MM:15

TIME-30 MIN

(1) Let x be the A. M. and y, z be two G. M.'s between any two positive numbers. Then, prove that

$$\frac{y^3 + z^3}{xyz} = 2.$$

(2) The sum of an infinite geometric series is 15 and the sum of the squares of these terms is 45.

Find the series.

(3) Prove that the sum to n terms of the series $11 + 103 + 1005 + \dots$ is $\frac{10}{9}(10^n - 1) + n^2$

(4) If $S_1, S_2, S_3, \dots, S_m$ are the sums of n terms of m A. P.'s whose first terms are $1, 2, 3, \dots, m$ and common differences are $1, 3, 5, \dots, (2m - 1)$ respectively. Show that $S_1 + S_2 + S_3 + \dots + S_m = \frac{mn}{2}(mn + 1)$

(5) Between 1 and 31 are inserted m A. M.'s so that the ratio of the 7th and $(m - 1)$ th means is 5:9.

Find the value of m .